

Math 175 - Exam 3, December 2, 2009

Name:\_\_\_\_\_

*Problem 1* (20 points). Evaluate the integral  $\int_C x e^y \, ds$  where  $C$  is portion of the circle  $x^2 + y^2 = 4$  going counterclockwise from  $(2, 0)$  to  $(\sqrt{2}, \sqrt{2})$ .

*Problem 2* (20 points). Evaluate  $\iiint_E (x^2 + y^2 + z^2)^2 dV$  where  $E$  is the region above the  $xy$ -plane and in between the spheres  $x^2 + y^2 + z^2 = 1$  and  $x^2 + y^2 + z^2 = 4$ .

*Problem 3* (20 points). Evaluate  $\int_C F \cdot d\mathbf{r}$ , where  $F(x, y, z) = yz\mathbf{i} + (x+1)z\mathbf{j} + ((x+1)y+1)\mathbf{k}$  and  $C$  is the curve given by  $r(t) = (\cos t, \sin t, t)$ , for  $0 \leq t \leq 2\pi$ .

*Problem 4* (20 points). Evaluate the integral  $\int_C -y^3 dx + x^3 dy$  where  $C$  is the curve oriented positively which is made of the line segment from  $(0,0)$  to  $(\sqrt{2},0)$ , the counterclockwise arc on  $x^2 + y^2 = 2$  from  $(\sqrt{2},0)$  to  $(1,1)$ , and also the line segment from  $(1,1)$  to  $(0,0)$ .

*Problem 5* (20 points). Find the curl and divergence of the vector field  $F(x, y, z) = e^x \mathbf{i} + e^{xy} \mathbf{j} + e^{xyz} \mathbf{k}$ .

*Problem 6* (Extra Credit - 10 points, no partial credit). Let  $f : \mathbb{R}^3 \rightarrow \mathbb{R}$  be the function  $f(x, y, z) = ze^{x^2+y^2+z^2}$ . Find a vector field  $G$  such that  $\operatorname{div} G = f$  and  $G(0, 0, 0) = \mathbf{i} + \mathbf{j}$ .