

Problem 1. Let V be the subspace in \mathbb{R}^4 given by all solutions to the following homogeneous system of linear equations:

$$\begin{aligned}2x_1 + 4x_2 - 6x_3 &= 0 \\x_1 + x_2 - x_3 + 3x_4 &= 0 \\x_1 - x_2 + 3x_3 + 9x_4 &= 0.\end{aligned}$$

1. Find a linearly independent set for V .
2. Find a spanning set for V .
3. Find a basis for V .
4. What is the dimension of V ?