## Math 2600/5600 - Linear Algebra - Fall 2015

## Extra Problems for Chapter 6

X12. (Algebraic derivation of $\operatorname{proj}_{x} y$ ) Prove algebraically that if $x \neq 0$ then $y-\alpha x \perp x$ if and only if $\alpha=\langle y, x\rangle /\langle x, x\rangle$.

X13. Find a basis for $\{(1,2,3,4),(-1,0,1,0)\}^{\perp}$ in $\mathbf{R}^{4}$ (by solving a system of linear equations).
X14. Prove that for any subset $S$ of $V, S^{\perp}=(\operatorname{span} S)^{\perp}$.

